



**Barcelona  
Supercomputing  
Center**

*Centro Nacional de Supercomputación*

# HPC electromagnetic modeling for geothermal reservoir characterization: Tenerife case study

***Octavio Castillo-Reyes<sup>1</sup>, Juanjo Ledo<sup>2</sup>, Perla Viña-Varas<sup>2</sup>,  
Pilar Queralt<sup>2</sup>***

<sup>1</sup> Geosciences Applications Group  
Barcelona Supercomputing Center (BSC)

<sup>2</sup> Institut Geomodels, Departament de Dinàmica de la Terra i de l'Oceà  
University of Barcelona (UB)

# Motivation

- Electromagnetic (EM) methods, both active and passive, help mapping the subsurface:
  - Electrical conductivity/resistivity as a **diagnostic physical property**
  - They are **sensitive to fluids**
  - Among the most **cost-effective** geophysical data
  - Effective both for **soil characterization and monitoring**
- Numerical simulations have become **inexpensive**:
  - Allow **validating our models** by direct comparison between data and synthetics



Oil & gas



Geothermal



Mineral exploration



Volcanology

# Geophysical EM modeling tool

- **PETGEM**

- Main driver is mostly written in Python
- High-order edge finite element method (**accurate**)
- Unstructured and adapted tetrahedral meshes (**flexible**)
- HPC support (**feasible runtime**)
- Open source under GPLv3 license (**free**)
- <https://petgem.bsc.es>



- Curl-curl formulation of the Maxwell's equations in frequency domain (EM fields are time-harmonic)

$$\nabla \times \mathbf{E} = i\omega\mu\mathbf{H} + \mathbf{K},$$

$$\nabla \times \mathbf{H} = \mathbf{J} + (\sigma + i\omega\epsilon)\mathbf{E}$$

$\mathbf{J}, \mathbf{K}$  = electric and magnetic sources

$i$  = imaginary unit

$\omega$  = angular frequency

$\mu$  = free-space magnetic permeability

$\epsilon$  = constant model permittivity

$\sigma$  = variable electric conductivity tensor

## Active-source EM

Controlled source electromagnetic method (CSEM)

$$\nabla \times \nabla \times \mathbf{E} - i\omega\mu\sigma\mathbf{E} = i\omega\mu\mathbf{J}$$

## Passive-source EM

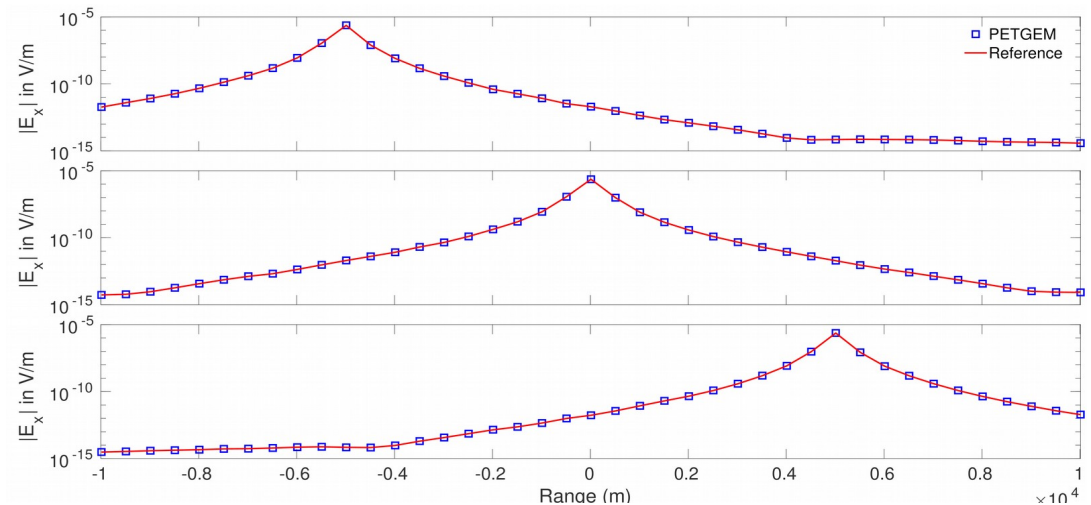
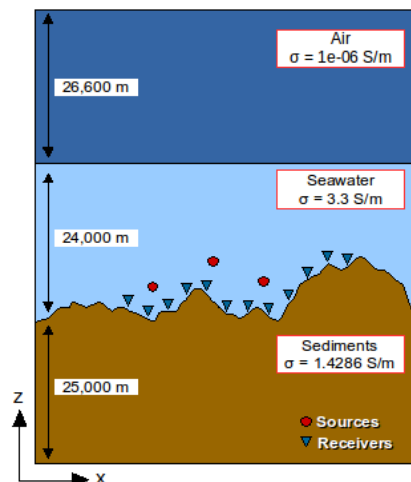
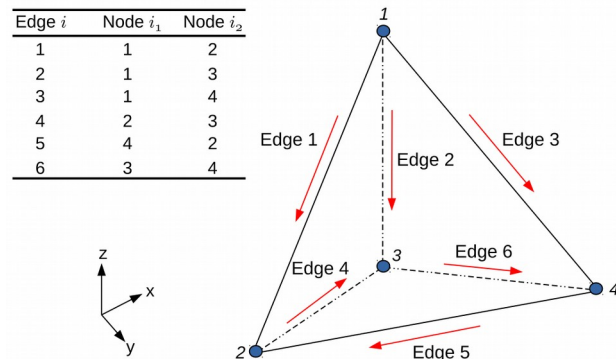
Magnetotelluric method (MT)

$$\nabla \times \nabla \times \mathbf{E} - i\omega\mu\sigma\mathbf{E} = 0$$

# Geophysical EM modeling tool

2018

Castillo-Reyes, O., de la Puente, J., Cela, J. M. (2018). **PETGEM: A parallel code for 3D CSEM forward modeling using edge finite elements**. Computers & Geosciences, vol 119: 123-136. [ISSN 0098-3004](#). Elsevier.



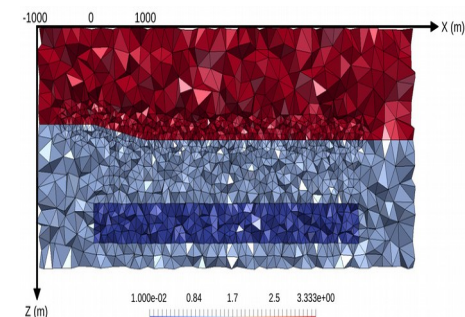
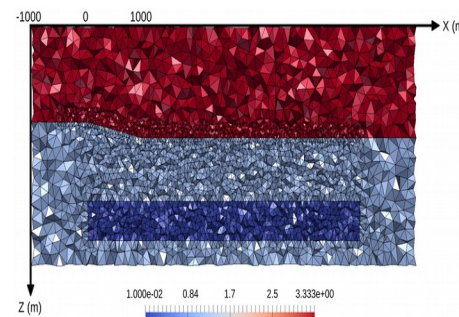
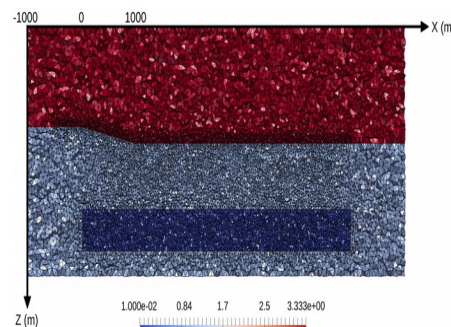
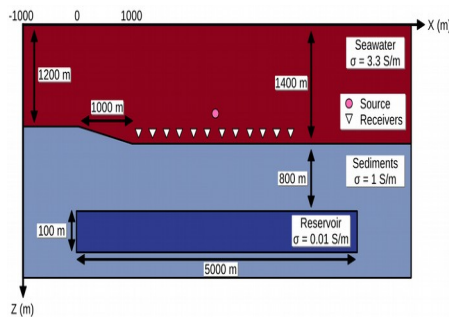
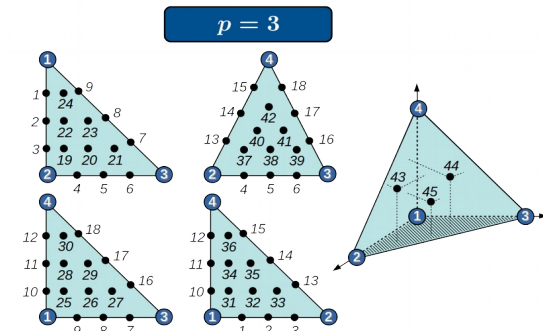
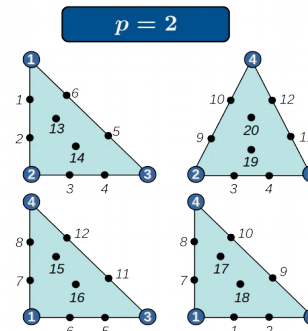
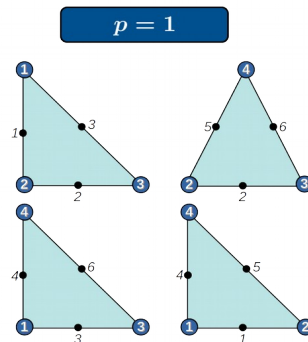
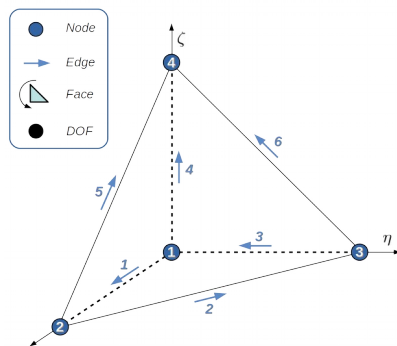


# Geophysical EM modeling tool

2018

2019

Castillo-Reyes, O., de la Puente, J., García-Castillo, L. E., Cela, J. M. (2019). **Parallel 3D marine controlled-source electromagnetic modeling using high-order tetrahedral Nédélec elements**. Geophysical Journal International, ggz285, vol 219: 39-65. ISSN 0956-540X.

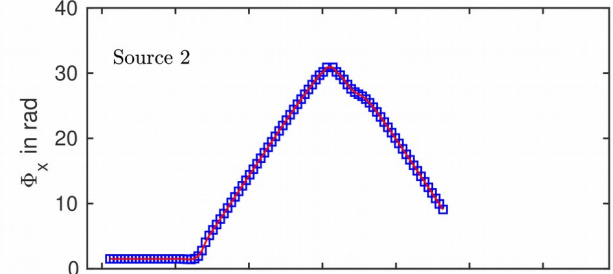
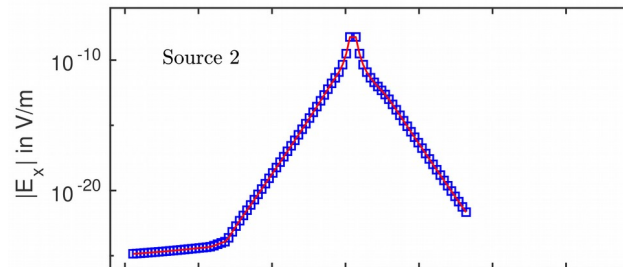
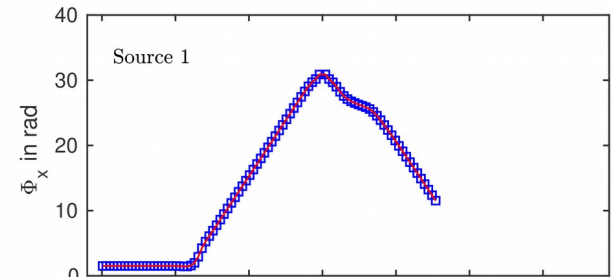
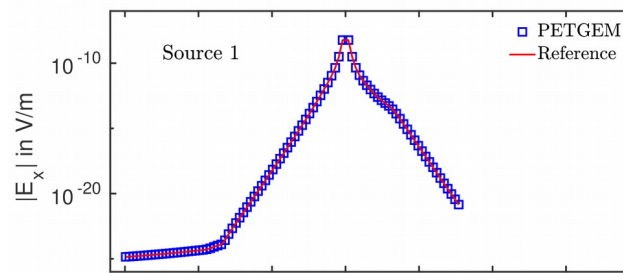
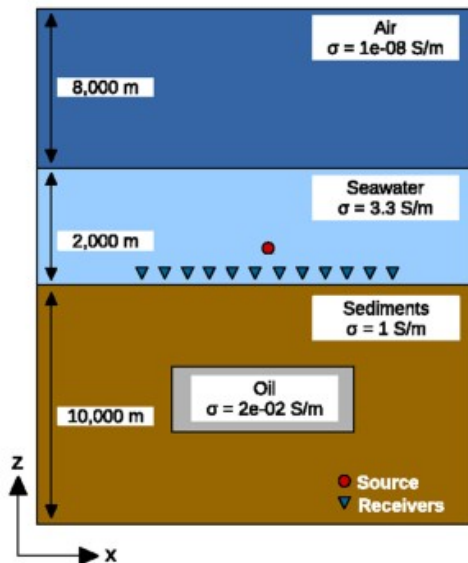


# Geophysical EM modeling tool

2018

2019

Castillo-Reyes, O., de la Puente, J., García-Castillo, L. E., Cela, J. M. (2019). **Parallel 3D marine controlled-source electromagnetic modeling using high-order tetrahedral Nédélec elements**. Geophysical Journal International, ggz285, vol 219: 39-65. ISSN 0956-540X.



# Geophysical EM modeling tool

2018

2019

2021 (a)

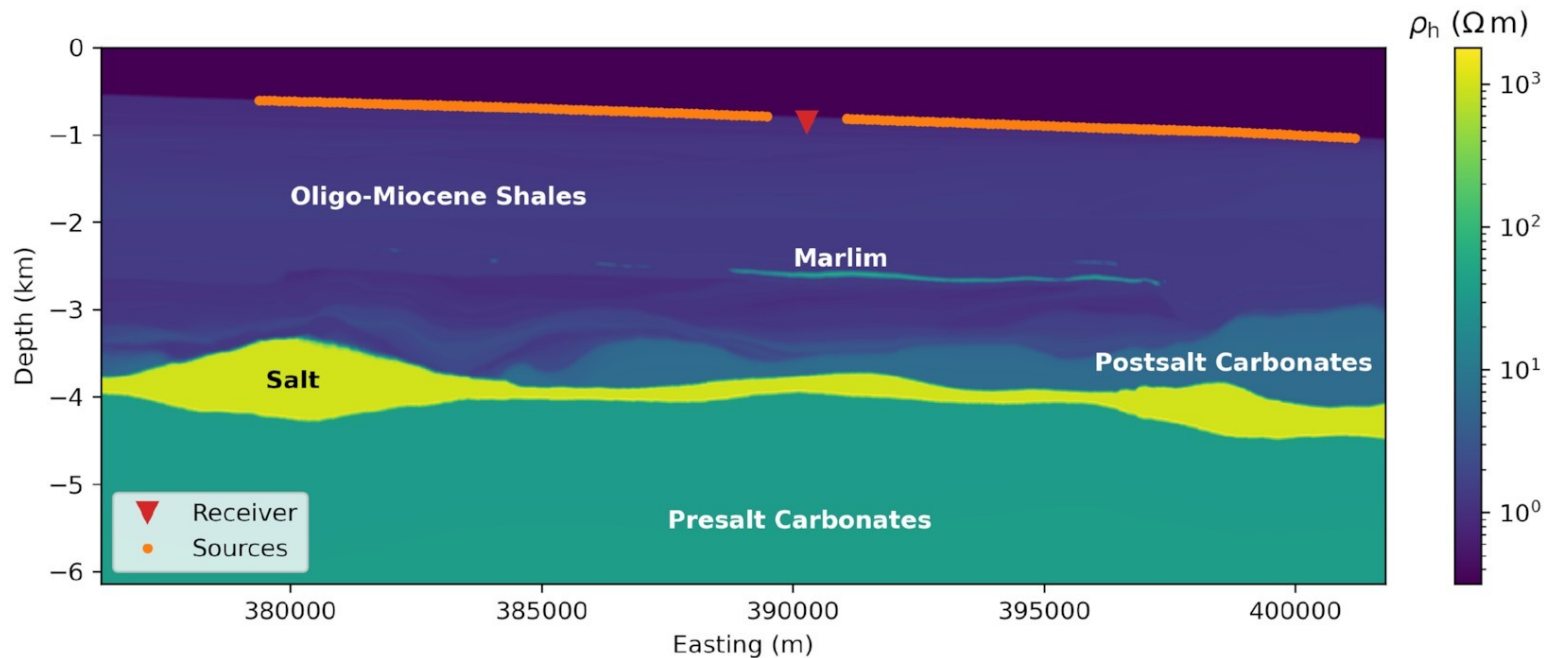
Werthmüller, D., Rochlitz, R., Castillo-Reyes, O., & Heagy, L. (2021). **Towards an open-source landscape for 3-D CSEM modelling**. *Geophysical Journal International*, 227(1), 644-659.

W/emg3d

simpeg

custEM

petgem



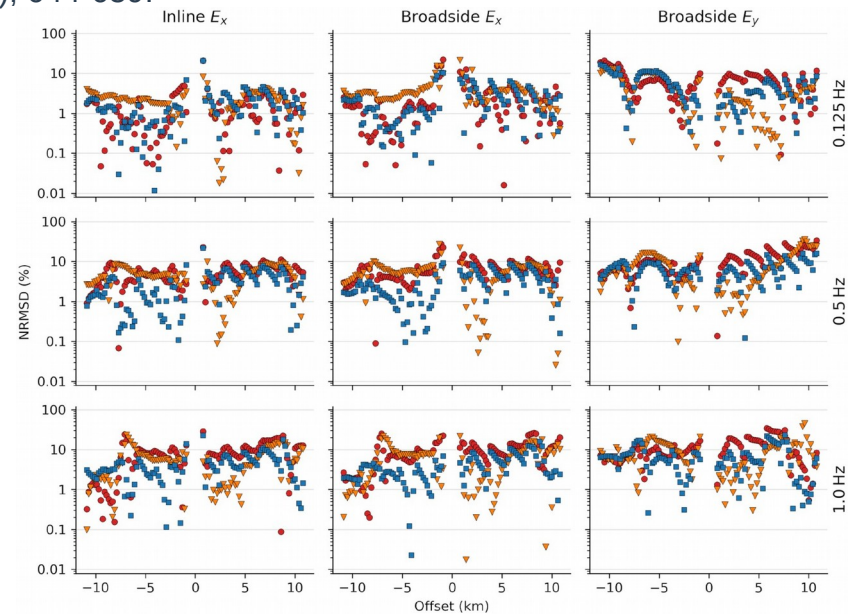
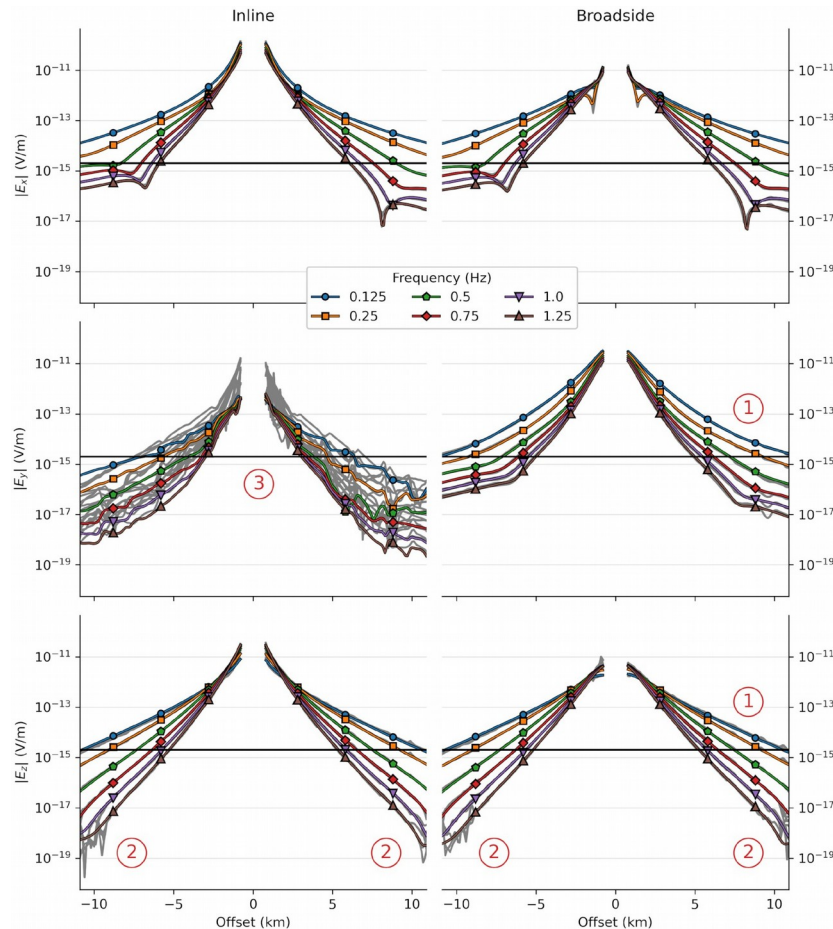
# Geophysical EM modeling tool

2018

2019

2021 (a)

Werthmüller, D., Rochlitz, R., Castillo-Reyes, O., & Heagy, L. (2021). **Towards an open-source landscape for 3-D CSEM modelling**. *Geophysical Journal International*, 227(1), 644-659.



■ emg3d—MR3D    ▼ custEM|PETGEM—MR3D    ● SimPEG—MR3D

Code	#Procs	Runtime (s)	Memory (GiB)	#dof
custEM	64	872	230.1	1918106
emg3d	1	1246	0.5	5998992
PETGEM	96	524	175.4	1918106
SimPEG	4	422	12.8	720146



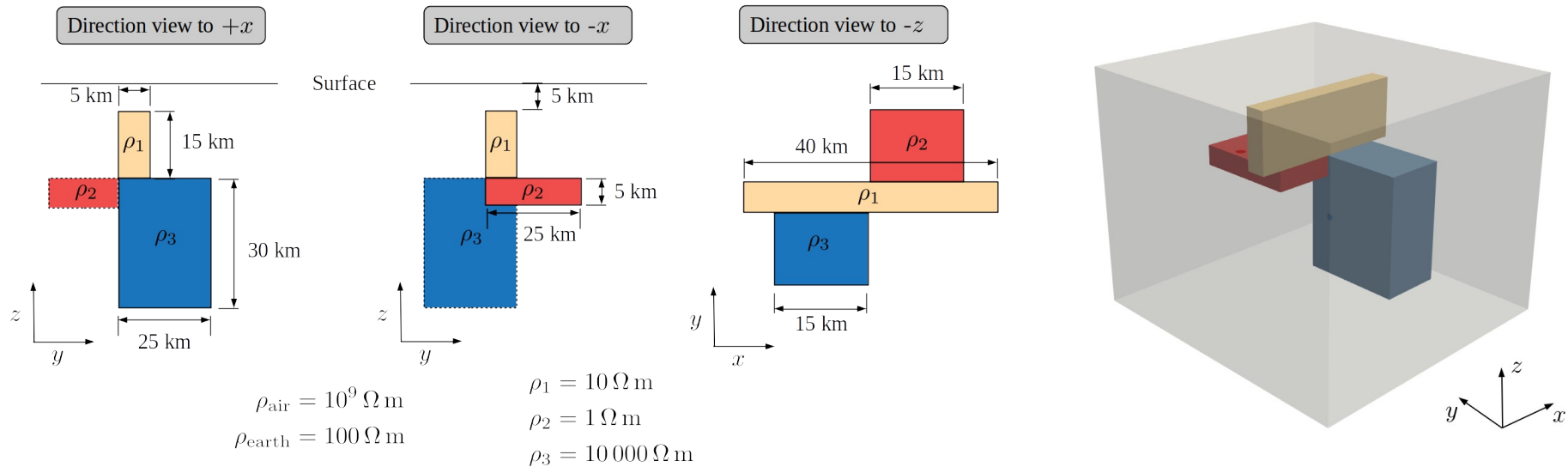
# Geophysical EM modeling tool

2018

2019

2021 (b)

Castillo-Reyes, O., Modesto, D., Queralt, P., Marcuello, A., Ledo, J., Amor-Martin, A., de la Puente, J., García-Castillo, L.E. (2021). **3D magnetotelluric modeling using high-order tetrahedral Nédélec elements on massively parallel computing platforms**. Submitted to Computers & Geosciences.



# Geophysical EM modeling tool

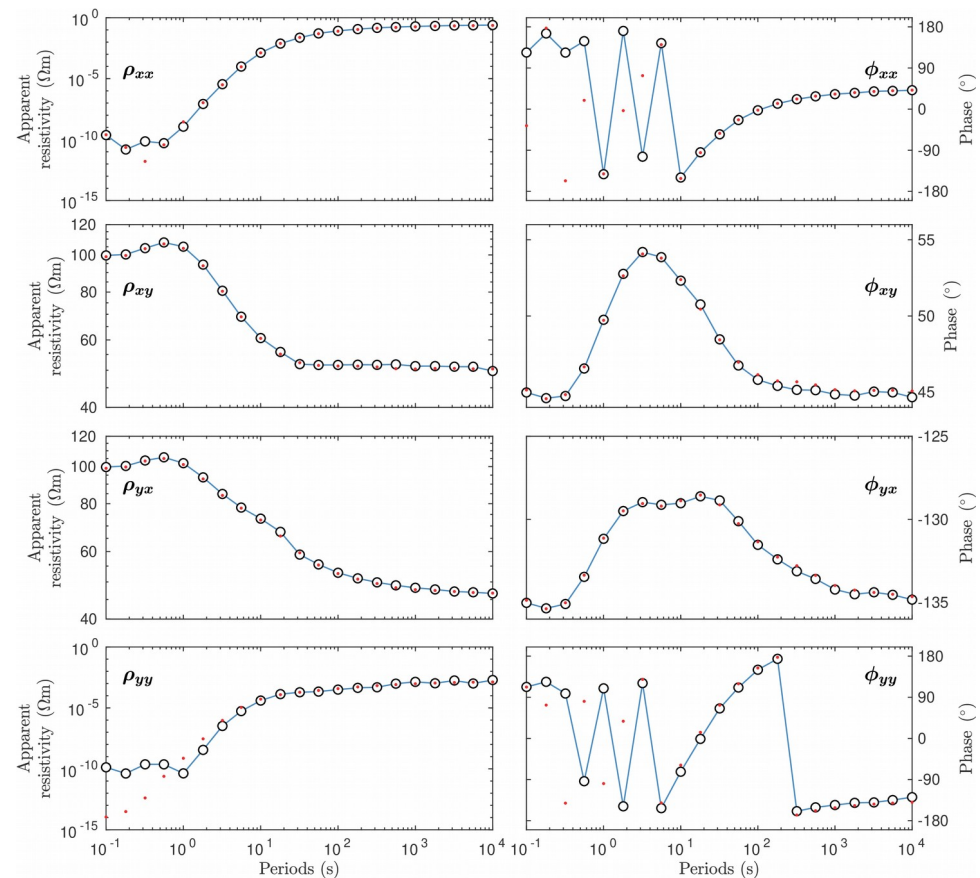
2018

2019

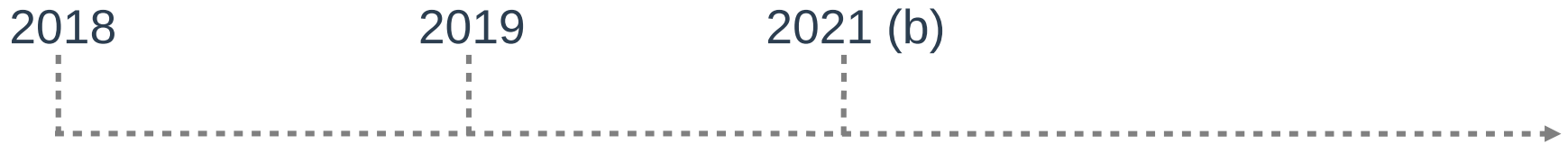
2021 (b)

Castillo-Reyes, O., Modesto, D., Queralt, P., Marcuello, A., Ledo, J., Amor-Martin, A., de la Puente, J., García-Castillo, L.E. (2021). **3D magnetotelluric modeling using high-order tetrahedral Nédélec elements on massively parallel computing platforms**. Submitted to Computers & Geosciences.

- Unstructured mesh adapted for **second-order** polynomials (2,774, 334 dofs)
- $\approx 14$  min of run-time using 240 CPUs and the MUMPS parallel solver
- **Excellent run-times**
  - Reference:  $\approx 57$  hrs
  - PETGEM:  $\approx 4.9$  hrs
- **Positive impact of adapted meshes** for each period



# Geophysical EM modeling tool



- Extensively validated on realistic models:
  - Active-source and passive-source
- Experience in this work-flow is crucial to **exploring useful underground resources**
- What is next?
- Transfer expertise from oil & gas to other **scenarios/applications**
  - **Geothermal energy**



# Geophysical EM modeling tool

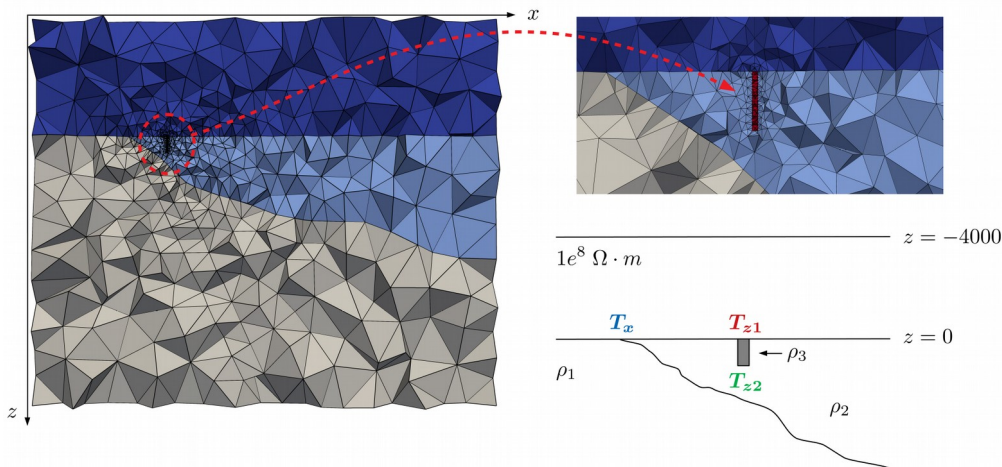
2018

2019

2021 (c)

Castillo-Reyes, O., Queralt, P., Marcuello, A., & Ledo, J. (2021). Land CSEM simulations and experimental test using metallic casing in a geothermal exploration context: Vallès Basin (NE Spain) case study. IEEE Transactions on Geoscience and Remote Sensing.

- Vallés Basin (NE, Spain) relevant region because several **geothermal anomalies** are present there
- Modeling in the presence of **metallic borehole**



Case label	$\rho_1$ (Basement)	$\rho_2$ (Sediments)	$\rho_3$ (Casing)
$T_x \beta \beta \beta$	$\beta$	$\beta$	$\beta$
$T_{z1} \beta \beta \beta$	$\beta$	$\beta$	$\beta$
$T_{z1} \beta \beta \gamma$	$\beta$	$\beta$	$\gamma$
$T_{z1} \beta \beta \delta$	$\beta$	$\beta$	$\delta$
$T_{z2} \beta \beta \gamma$	$\beta$	$\beta$	$\gamma$
$T_{z2} \beta \beta \delta$	$\beta$	$\beta$	$\delta$
$T_x \alpha \beta \gamma$	$\alpha$	$\beta$	$\gamma$
$T_{z1} \alpha \beta \delta$	$\alpha$	$\beta$	$\delta$
$T_{z2} \alpha \beta \gamma$	$\alpha$	$\beta$	$\gamma$
$T_x \alpha \beta \delta$	$\alpha$	$\beta$	$\delta$
$T_{z1} \alpha \beta \gamma$	$\alpha$	$\beta$	$\gamma$
$T_{z2} \alpha \beta \delta$	$\alpha$	$\beta$	$\delta$
$\alpha = 1000 \quad \beta = 20 \quad \gamma = 0.005 \quad \delta = 0.001$			

# Geophysical EM modeling tool

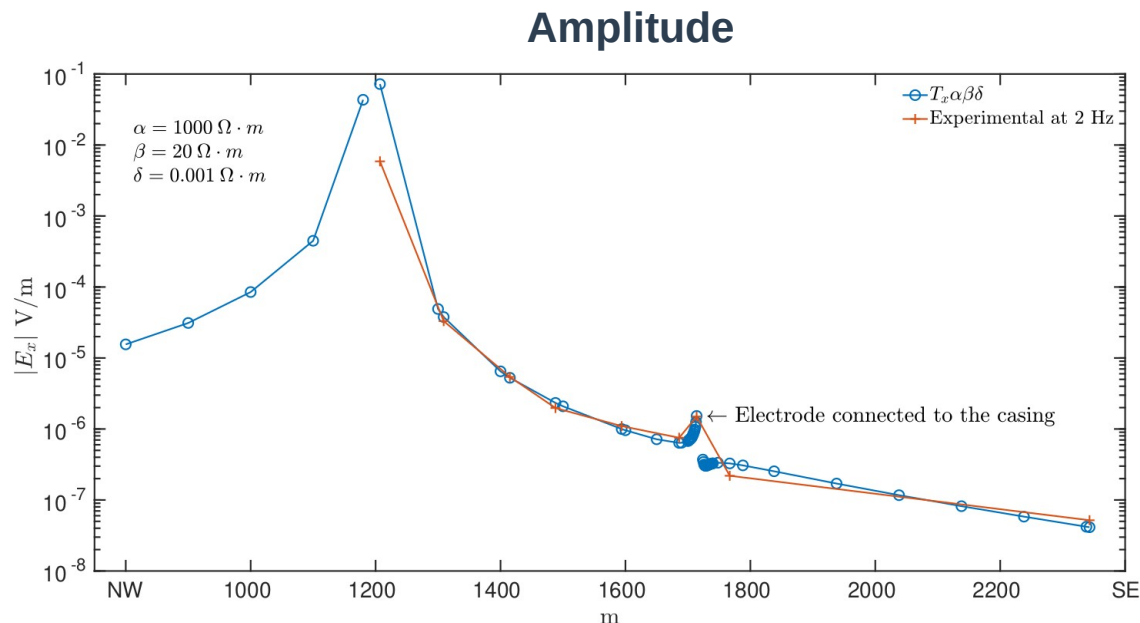
2018

2019

2021 (c)

Castillo-Reyes, O., Queralt, P., Marcuello, A., & Ledo, J. (2021). Land CSEM simulations and experimental test using metallic casing in a geothermal exploration context: Vallès Basin (NE Spain) case study. IEEE Transactions on Geoscience and Remote Sensing.

- Comparison between experimental data in-situ of the Vallés Basin profile compared with synthetics obtained with **PETGEM**



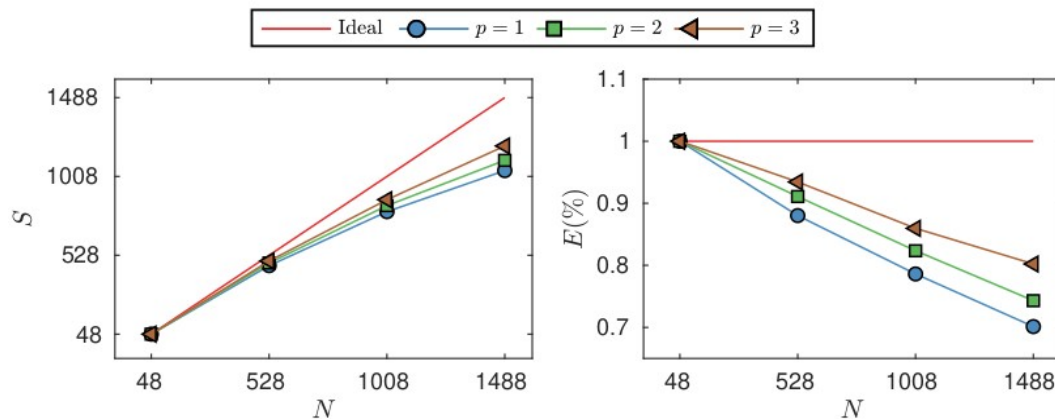


# Geophysical EM modeling tool



Castillo-Reyes, O., Queralt, P., Marcuello, A., & Ledo, J. (2021). **Land CSEM simulations and experimental test using metallic casing in a geothermal exploration context: Vallès Basin (NE Spain) case study.** IEEE Transactions on Geoscience and Remote Sensing.

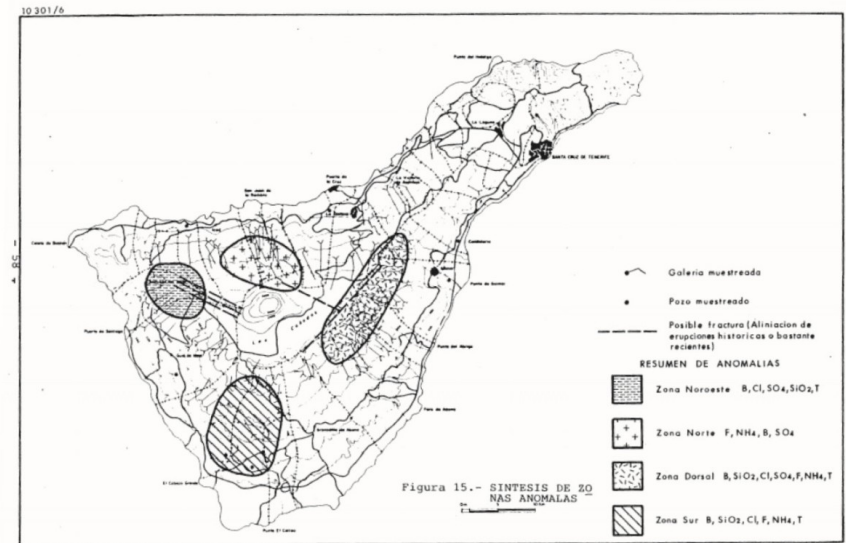
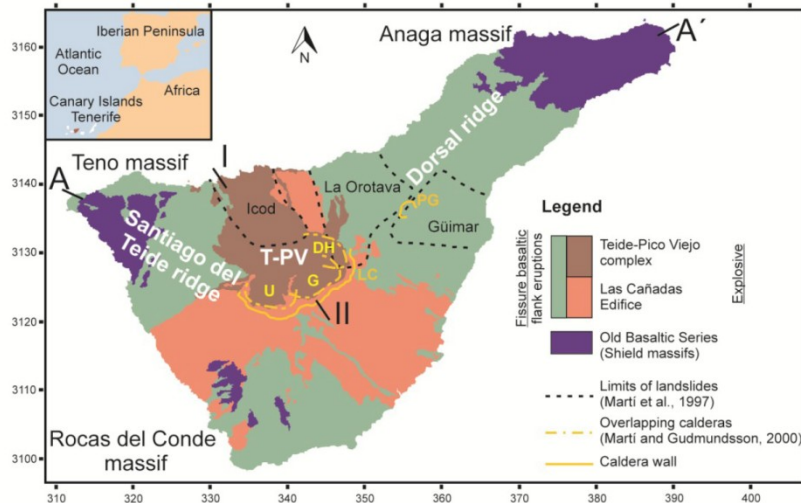
- **Excellent** and **competitive** run-times (**solver** is the main **discriminator**)
- Although **higher-order** polynomials increase the run-time, they offer **better parallel efficiency** ratios
- Computational efficiency depends of the **solver-type** and the **input model**



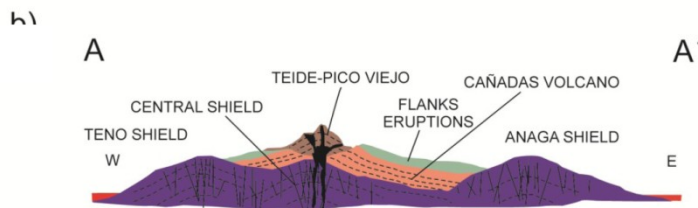
CPU	48	528	1008	1488
$p = 1$ with 1 249 109 dof				
Run-time	98.71	10.19	5.97	4.54
$S$	—	9.68	16.53	21.74
$E$ (%)	—	.8806	.7861	.7013
$p = 2$ with 6 697 994 dof				
Run-time	392.18	39.14	22.67	17.02
$S$	—	10.01	17.29	23.04
$E$ (%)	—	91.09	82.35	74.31
$p = 3$ with 19 454 679 dof				
Run-time	985.28	95.85	54.58	39.62
$S$	—	10.27	18.05	24.86
$E$ (%)	—	93.44	85.96	80.22

# Tenerife island

- **Complex geological history:** alternation in both **constructive** and **destructive** episodes
- Target of **geothermal exploration** studies since the 80s

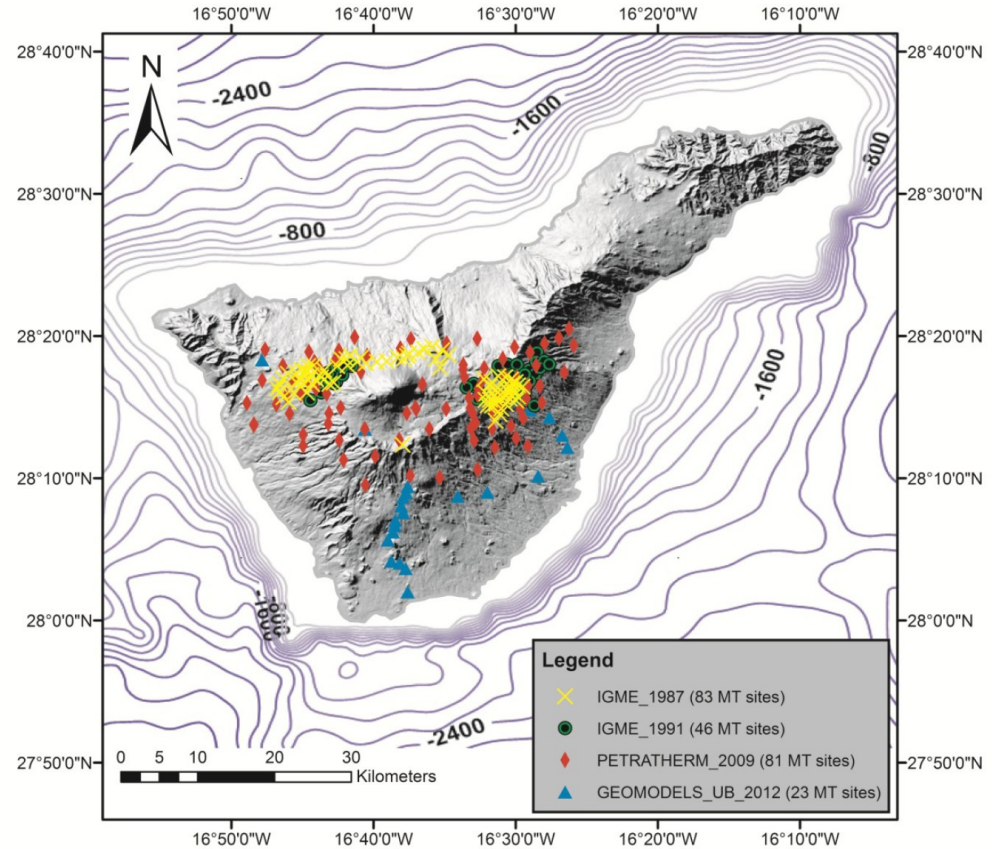


Water anomalies reported by the Geological and Mining Institute of Spain (IGME 1983-1993)



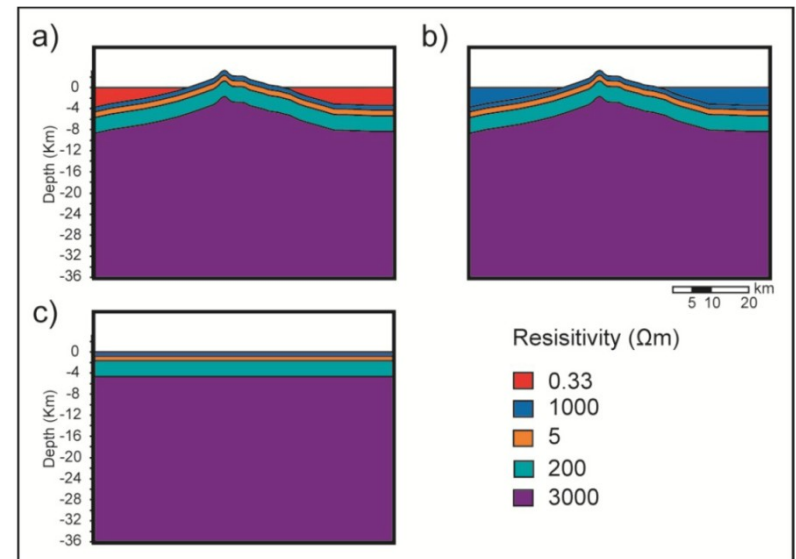
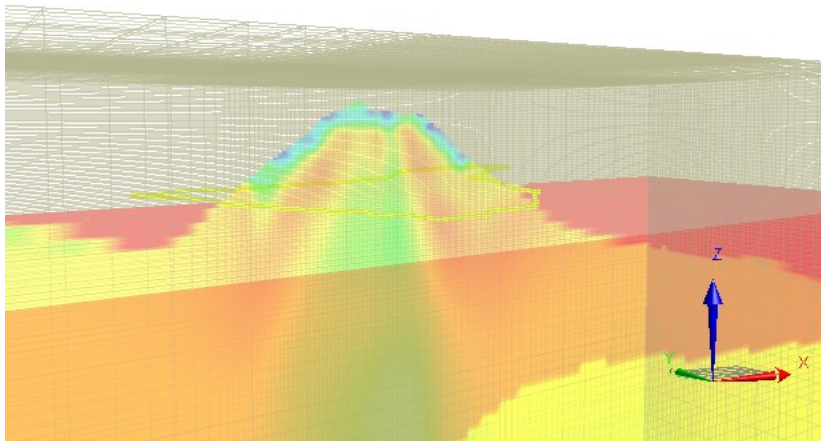
# Tenerife island

- **233 MT sites** in total
- **129 digitalized** from old MT surveys
- **3D** data dimensionality
- **Data distorted** by:
  - Steep topography
  - Surrounding ocean
- **Challenging** from a **numerical modeling** perspective



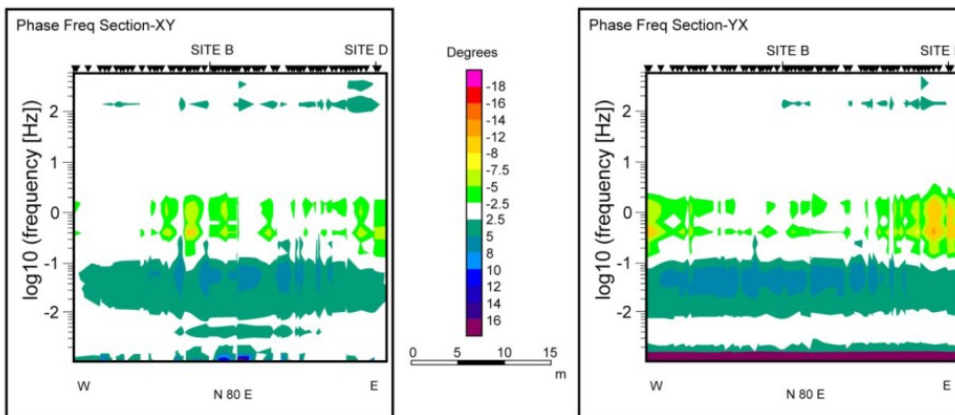
# Tenerife island

- Steep topography and the surrounding ocean: **effect on the MT data**
- Three different conceptual models:
  - (a) **Ocean model**: including topography and ocean
  - (b) **Land model**: including topography but not the conductive surrounding model
  - (c) **1D model**: no topography, neither ocean

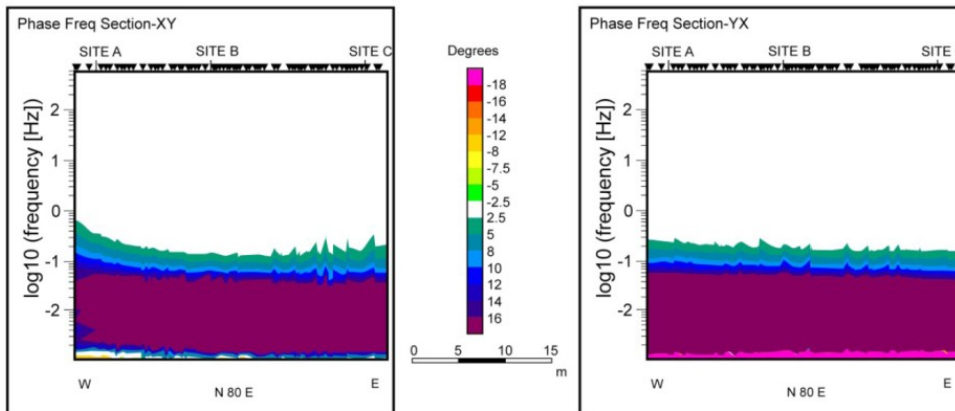


# Tenerife island

- Steep topography and the surrounding ocean: **effect on the MT data**
- **MT data strongly distorted** by the presence of the steep topography and the surrounding ocean at **frequencies lower than 0.1 Hz**



Pseudosection plots of phase difference between land and 1D model.

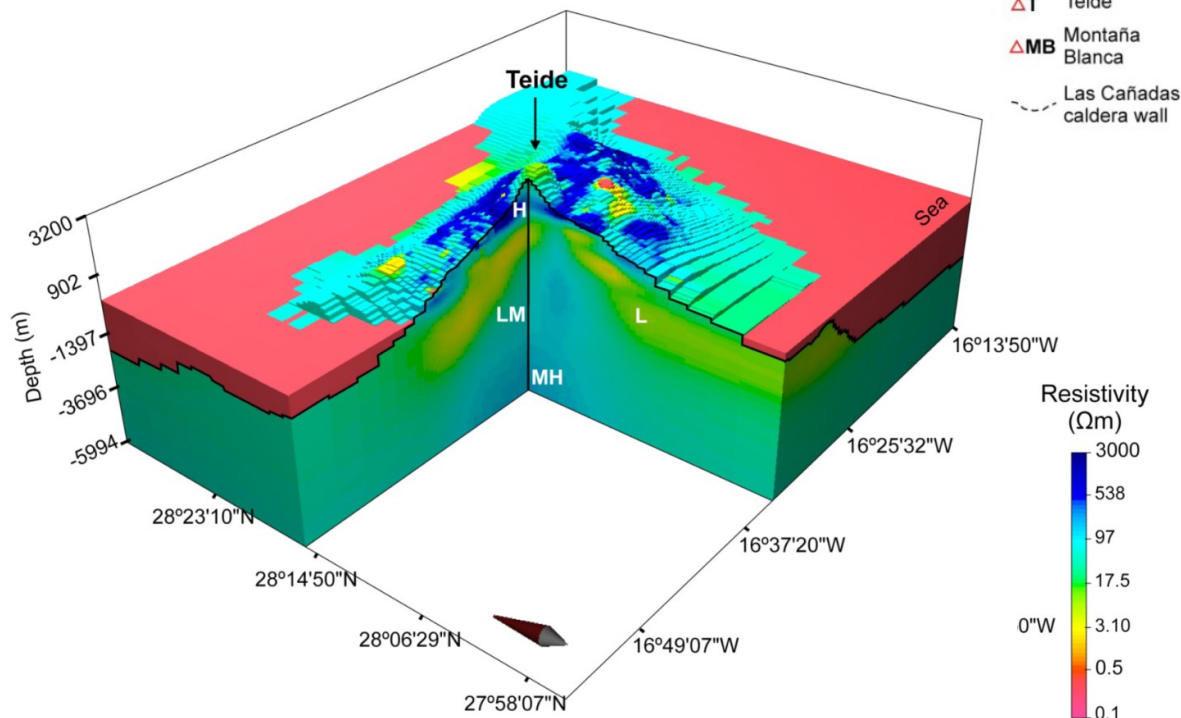


Pseudosection plots of phase difference between land and sea model.

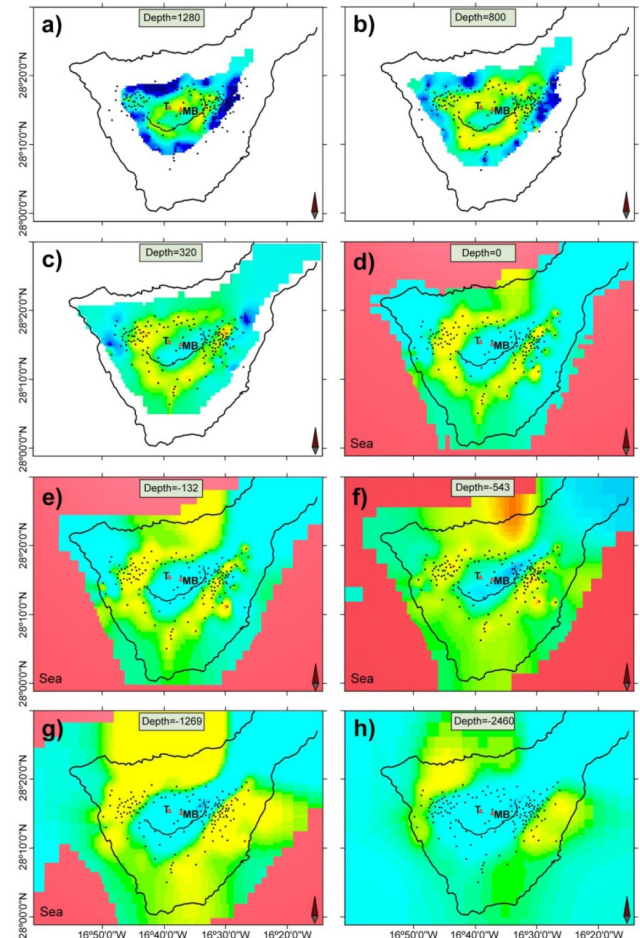


# Tenerife island: 3D resistivity model

- Most striking feature: **Low resistivity layer (L)** located in the central part of the island
- Low resistivity layer (L) **characterized by**:
  - Resistivity values **lower** than 10 Ohm.m
  - **Ring-shape open** in the central part of the island, in
  - agreement with the location of the Las Cañadas Caldera



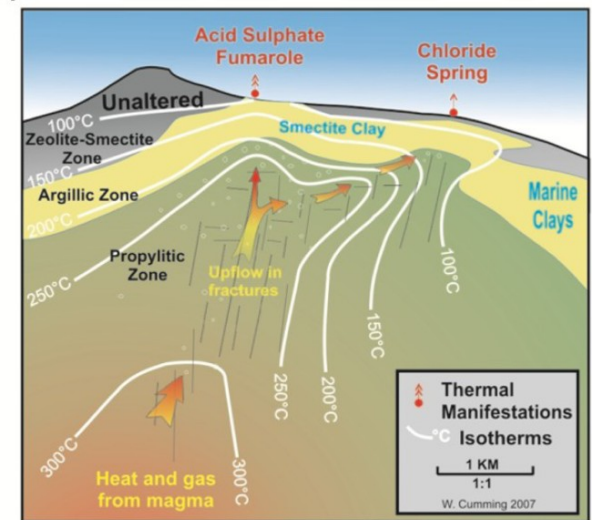
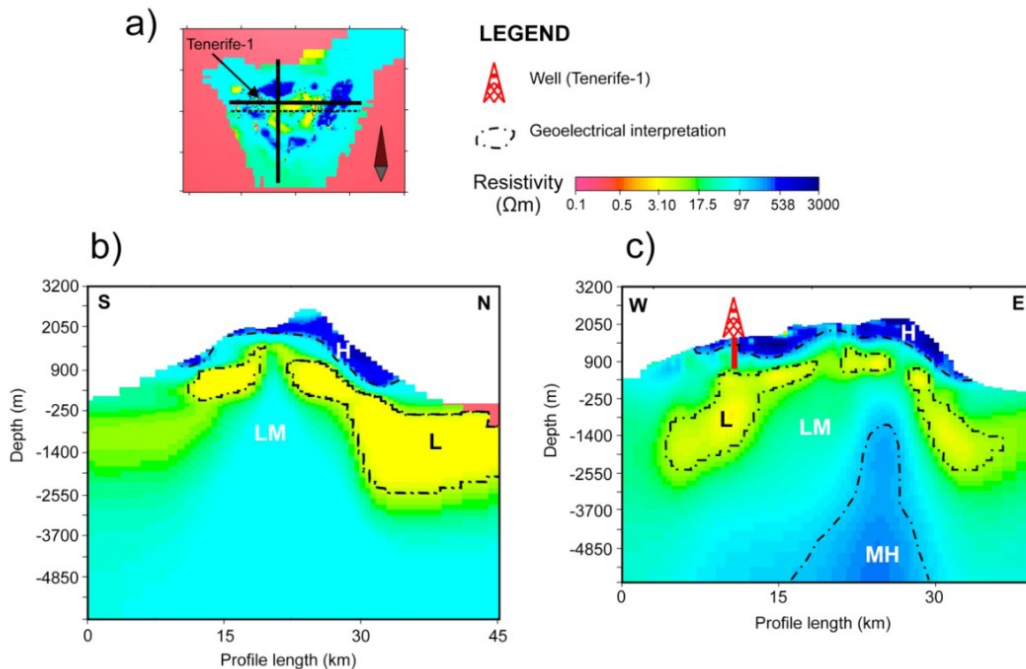
- MT site
- △T Teide
- △MB Montaña Blanca
- Las Cañadas caldera wall



# Tenerife island: geothermal system

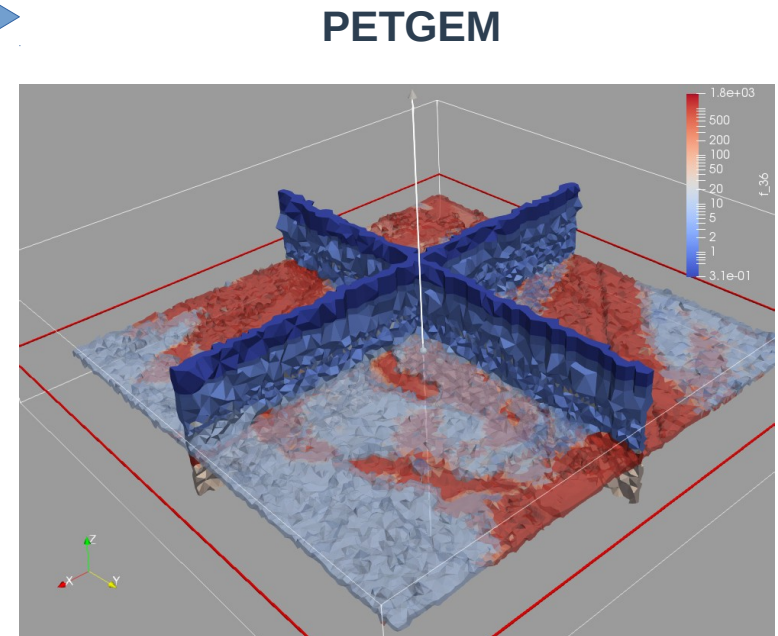
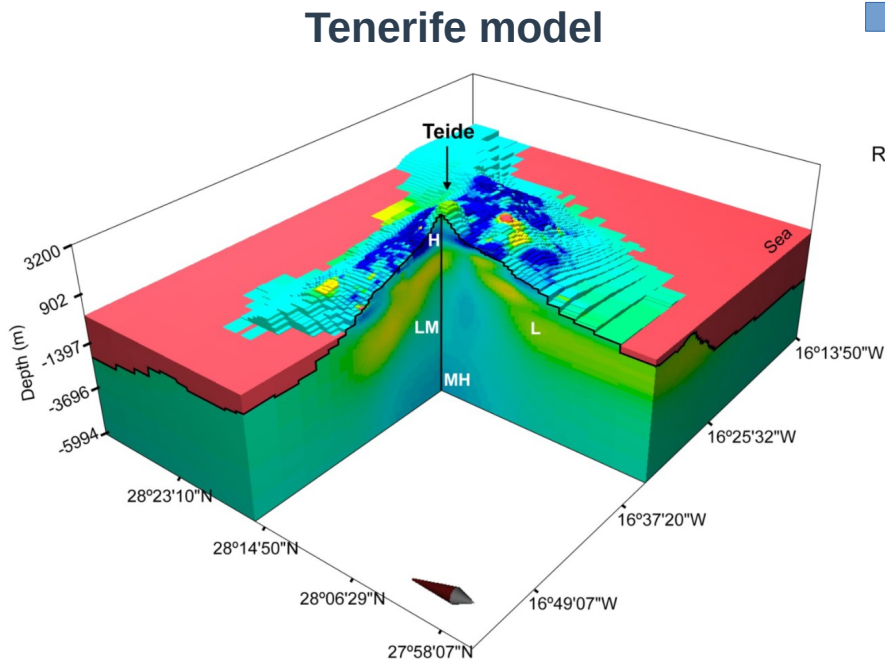
- Resistivity distribution, from shallow to depth:
  - H: **High** resistivities, 1000 Ohm.m
  - L: **Low** resistivity layer, <10 Ohm.m
  - LM: **Low-medium** resistivities, 20-100 Ohm.
  - MH: **Medium-high** resistivities, 100-500 Ohm

Goelectrical distribution of a **high-temperature geothermal system**



# Tenerife island: MT/CSEM modeling

- PETGEM computations to analyze MT/CSEM responses:
  - **Experimental data** to build the computational domain
  - Finite difference grid to finite element grid (**adapted mesh**)
  - Compare **synthetic** EM responses against **experimental** responses
- **Improve our knowledge** about the Tenerife model:
  - Previous MT results allow us to **verify, control, and restrict** the CSEM responses
  - Confirm the role of **electromagnetic geophysical**



# Conclusions

- **A triple helix approach** based on high-order basis, *hp*-adapted meshes, and HPC can be **extremely competitive** for the solution of realistic and complex 3-D MT/CSEM models
  - Full 3-D analysis of EM fields
  - Run-time, accuracy, speed-up and parallel efficiency
- **Know-how** is fundamental for **future** modeling tasks and **developments** (e.g. EM inversion routines)
  - **Suitable workflow** for many and diverse applications (oil & gas, geothermal energy)
  - Transfer expertise to **non-conventional scenarios**
  - Critical role in solving the next generation of geoscience problems: complex, multidisciplinary, and **require collaboration**

# Conclusions

- PETGEM uses in **conventional/non-conventional** energy surveys:
  - **Prior** to drilling;
    - Study sensitivity to different reservoir configurations
    - Plan data acquisition strategies
    - If data is available: obtain conductivity maps (i.e. find fluids)
  - **After** drilling:
    - Monitor fluid leaks





**Barcelona  
Supercomputing  
Center**

*Centro Nacional de Supercomputación*

# Thank you!

[octavio.castillo@bsc.es](mailto:octavio.castillo@bsc.es)